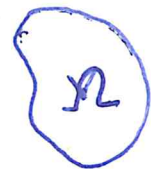

$$\int_0^L u' dx = u(L) - u(0)$$

$$\int_V \nabla \cdot u = \oint_{\partial V} u \cdot n dS$$

$$V = \int_{\Omega(t)} dV \Rightarrow \dot{V} = \frac{d}{dt} \int_{\Omega(t)} dV = \frac{d}{dt} \int_{\Omega_0} J dV_0$$

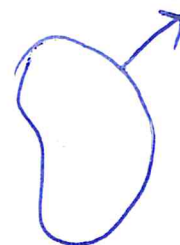
$$= \int_{\Omega_0} \nabla_0 \cdot u |J| dV_0 = \int_{\Omega_0} \nabla_0 \cdot u dV = \oint_{\partial \Omega_0} u \cdot n dS$$

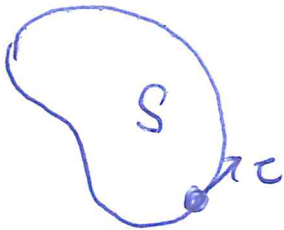
$$V = \frac{4}{3} \pi R^3$$

$$\dot{V} = \frac{4\pi R^2}{3} \dot{R}$$

$\dot{R} \uparrow v_{\text{radiale}}$

$$dV = 4\pi R^2 v dt$$





$$\int_{\partial S} u \cdot \tau \, d\ell = \int_S (\nabla \times u) \cdot n \, d\sigma \Rightarrow \frac{1}{S} \int \omega \cdot n \, dS = \bar{\omega}$$

$$\bar{\omega} = \frac{1}{S} \int_{\partial S} u \cdot \tau \, d\ell$$

$$\int_V \frac{\partial u_i}{\partial x_i} \, dV = \int_{\partial V} u_i n_i$$

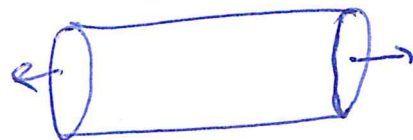
$$\nabla \cdot \phi \mathbf{I} = \nabla \phi$$

$$\phi \delta_{ij} = \phi_{ij}$$

$$\int_V \frac{\partial T_{ij}}{\partial x_j} \, dV = \int_{\partial V} T_{ij} n_j \, dV$$

$$\frac{\partial \phi_{ij}}{\partial x_j} = \frac{\partial \phi}{\partial x_j} \delta_{ij}$$

$$\int_V \frac{\partial \phi}{\partial x_i} \, dV = \int_{\partial V} \phi n_i \, dS$$



$$\int \partial \phi = \int_{\partial V} \phi n_i \, dS + \int_{\partial V} \phi n_i \, dV$$



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$$\int_V \nabla_{x_k} dV = \int_{\partial V} n_k dS$$

$$\int_V \epsilon_{ijk} \frac{\partial u_k}{\partial x_j} dV = \int_{\partial V} \epsilon_{ijn} u_k m_j dS$$

# ES 5

$$\mu = (Sx_2, 0, 0) \quad \mu_1 = Sx_2 \quad \mu_2 = 0 \quad \mu_3 = 0$$

MOTO PIANO

$$(\nabla \mu)_{ij} = \frac{\partial \mu_i}{\partial x_j} \Rightarrow \begin{cases} (\nabla \mu)_{11} = \frac{\partial \mu_1}{\partial x_1} = 0 & (\nabla \mu)_{21} = \frac{\partial \mu_1}{\partial x_2} \\ (\nabla \mu)_{12} = \frac{\partial \mu_1}{\partial x_2} = S & (\nabla \mu)_{22} = \frac{\partial \mu_2}{\partial x_2} \end{cases}$$

$$\nabla \mu = \begin{bmatrix} 0 & S \\ 0 & 0 \end{bmatrix}$$

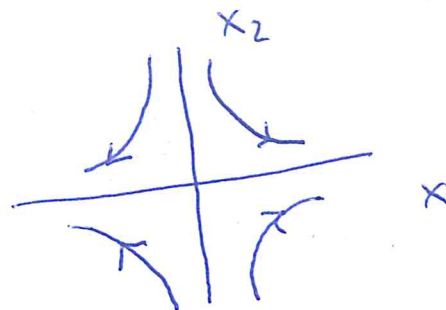
$$E_{ij} = \frac{1}{2} \left( \frac{\partial \mu_i}{\partial x_j} + \frac{\partial \mu_j}{\partial x_i} \right) \Rightarrow \begin{cases} E_{11} = \frac{\partial \mu_1}{\partial x_1} = 0 & E_{12} = \frac{1}{2} \left( \frac{\partial \mu_1}{\partial x_2} + \frac{\partial \mu_2}{\partial x_1} \right) \\ & = S/2 \\ E_{21} = \frac{1}{2} \left( \frac{\partial \mu_2}{\partial x_1} + \frac{\partial \mu_1}{\partial x_2} \right) = S/2 & E_{22} = \frac{\partial \mu_2}{\partial x_2} \end{cases}$$

$$E = \frac{1}{2} (\nabla \mu + \nabla \mu^T) = \begin{bmatrix} 0 & S/2 \\ S/2 & 0 \end{bmatrix}$$

$$\Omega_{ij} = \frac{1}{2} \left( \frac{\partial \mu_i}{\partial x_j} - \frac{\partial \mu_j}{\partial x_i} \right) \Rightarrow \begin{cases} \Omega_{11} = 0 & \Omega_{12} = \frac{1}{2} \left( \frac{\partial \mu_1}{\partial x_2} - \frac{\partial \mu_2}{\partial x_1} \right) \\ & = 0 \\ \Omega_{21} = -S/2 & \Omega_{22} = 0 \end{cases}$$

$$\Omega = \frac{1}{2} (\nabla \mu - \nabla \mu^T) = \begin{bmatrix} 0 & S/2 \\ -S/2 & 0 \end{bmatrix}$$

$$u = (ax_1, -ax_2, 0) \quad \text{CAMPO PIANO}$$



$$(\nabla u)_{11} = \frac{\partial u_1}{\partial x_1} = a$$

$$(\nabla u)_{21} = \frac{\partial u_2}{\partial x_1} = 0$$

$$(\nabla u)_{12} = \frac{\partial u_1}{\partial x_2} = 0$$

$$(\nabla u)_{22} = \frac{\partial u_2}{\partial x_2} = -a$$

$$\nabla u = \begin{bmatrix} a & 0 \\ 0 & -a \end{bmatrix} = E$$

$$E_{11} = \frac{\partial u_1}{\partial x_1} = a$$

$$E_{12} = \frac{1}{2} \left( \frac{\partial u_1}{\partial x_2} + \frac{\partial u_2}{\partial x_1} \right) = 0$$

$$E_{21} = \frac{1}{2} \left( \frac{\partial u_2}{\partial x_1} + \frac{\partial u_1}{\partial x_2} \right) = 0$$

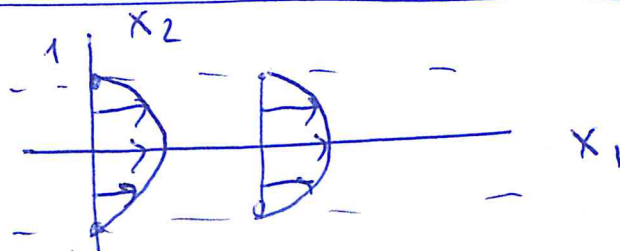
$$E_{22} = \frac{\partial u_2}{\partial x_2} = -a$$

$$\Omega_{11} = 0 \quad \Omega_{12} = 0$$

$$\Omega = \nabla u - E = 0$$

$$\Omega_{21} = 0 \quad \Omega_{22} = 0$$

$$u = (S(x_2^2 - 1), 0)$$



$$(\nabla u)_{11} = \frac{\partial u_1}{\partial x_1} = 0$$

$$(\nabla u)_{21} = \frac{\partial u_1}{\partial x_1} = 0$$

$$\nabla u = \begin{bmatrix} 0 & 2Sx_2 \\ 0 & 0 \end{bmatrix}$$

$$(\nabla u)_{12} = \frac{\partial u_1}{\partial x_2} = 2Sx_2$$

$$(\nabla u)_{22} = \frac{\partial u_2}{\partial x_2} = 0$$